# $\mathrm{HP}_{4}{ }^{-}$and $\left(\mathrm{CH}_{2}\right) \mathrm{P}_{3}{ }^{-}$Anions Form Four-membered Rings with an Allyl Moiety An ab initio/NMR study 

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Received: 7 October 1999/ Accepted: 21 January 2000/ Published: 28 February 2000


#### Abstract

On the energy hypersurfaces of the anions $\mathrm{HP}_{4}{ }^{-}$and $\mathrm{CH}_{2} \mathrm{P}_{3}{ }^{-}$at the RMP2(fc) $/ 6-31+\mathrm{G}(\mathrm{d})$ level, the isomers with triphosphaallyl moiety are the lowest energy structures. For these free $1-\mathrm{X}-2,4-$ $\left(\mathrm{P}_{\mathrm{B}}\right)_{2}-3-\mathrm{P}_{\mathrm{A}}^{-}$anions characteristic ${ }^{31} \mathrm{P}$ NMR chemical shifts, $?^{31} \mathrm{P}$, are predicted to be (for $\mathrm{X}=\mathrm{PH}, \mathbf{1}$, $\delta^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{A}}\right)=517, \delta^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{B}}\right)=424$, and $\delta^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{X}}\right)=50$; for $\left.\mathrm{X}=\mathrm{CH}_{2}, 4, \delta^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{A}}\right)=611, \delta^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{B}}\right)=450\right)$. The observed $\delta_{\text {exp }}{ }^{31} \mathrm{P}$ values for $\mathrm{HP}_{4}^{-}(\mathrm{Na} / \mathrm{K}, \mathrm{DME})$ completely disagree with the $\delta^{31} \mathrm{P}$ calculated at GIAO/ MP2/6-311+G(d) //RMP2(fc) /6-31+G(d) for structure 1. The rotational average of the phosphinidyltriphosphirene structures $\left(\mathrm{P}_{3}-\mathrm{PH}^{-}, 3\right)$ agree better with the $\delta_{\text {exp }}{ }^{31} \mathrm{P}$ than those with a bicyclo[1.1.0]hydrogentetraphosphanide backbone, 2. MO analysis can rationalize the extreme endo/ exo effect $\left(\Delta \delta^{31} \mathrm{P}=455 \mathrm{ppm}\right)$ on the chemical shift in the exocyclic PH group of $\mathbf{3}$. The lowest energy geometry of the anion $\mathbf{3}$ has $\mathrm{E}_{\text {rel }}$ of $31 \mathrm{~kJ} \mathrm{~mol}^{-1}$ relative to $\mathbf{1}$. The most favored $\mathbf{3}+\mathrm{Na}^{+}$structure is only $15 \mathrm{~kJ} \mathrm{~mol}^{-1}$ above the lowest energy $\mathrm{HP}_{4} \mathrm{Na}$ minimum, $2+\mathrm{Na}^{+}$with $\mathrm{Na}^{+}$in endo and H in exo orientation of the bicyclo- $\mathrm{P}_{4}$ framework ( $\mathrm{E}_{\text {rel }}$ of $\mathbf{1}+\mathrm{Na}^{+}$is $13 \mathrm{~kJ} \mathrm{~mol}^{-1}$ ). In most $\mathrm{HP}_{4} \mathrm{Na}$ structures the $\mathrm{Na}^{+}$ changes the ${ }^{31} \mathrm{P}$ NMR chemical shifts towards higher field with respect to the bare anions.


Keywords Ab initio calculations, Phosphorus heterocycles, Small ring systems, ${ }^{31} \mathrm{P}$ NMR

## Introduction

On the way from the perfect deltahedron, $\mathrm{P}_{4}\left(\mathrm{~T}_{\mathrm{d}}\right)$-- to polyphosphanes the intermediate species with less triangles has enticed various experimental and theoretical studies.[13] The $\mathrm{HP}_{4}{ }^{-}$anion attracted special interest due to its puzzling ${ }^{31} \mathrm{P}$ NMR chemical shift and the disagreement between

[^0]theoretical [4] and empirical [5] assignment of the P-H orientation (empirical endo vs theoretical exo preference) of bicyclo[1.1.0]tetraphosphanide (2endo and 2exo in Figures 1 and 2). The reported NMR chemical shift of the anionic phosphorus in $\mathrm{HP}_{4}^{-}(71.3 \mathrm{ppm})$ is about in the middle of the range of phosphanides (with formal $\sigma^{2}-\mathrm{P}$ moiety): -335 for solvated ${ }^{\text {t }} \mathrm{BuPHLi}$ to +732 for $\left({ }^{( } \mathrm{Bu}_{3} \mathrm{SiP}\right)_{2} \mathrm{P} \mathrm{Na}$ (solv). Furthermore $\delta^{31} \mathrm{P}$ of $\mathrm{HP}_{4}(\mathrm{Na} / \mathrm{K})$ is similar to that of the phospholide anion,[6] cyclo-(CH) ${ }_{4} \mathrm{P}^{-}(77.2 \mathrm{ppm})$. In this context the structural assignment to a bicycle is questionable. A monocyclic structure with an allylic -PPP- moiety, characterized by a 3 center $\pi$ bond, appears to be a reasonable alternative. Recent experimental research in phosphaallyls shows that the

Figure 1 Relative energies at MP2(fc)/6-31+G(d) in $k J$ $\mathrm{mol}^{-1}$ of $\mathrm{HP}_{4}^{-}$and $\mathrm{CH}_{2} \mathrm{P}_{3}^{-}$ anion structures. The high energy isomers (linear H $P P P P^{-}, E_{\text {rel }}=119 \mathrm{~kJ} \mathrm{~mol}^{-1}$ and the 1-phosphinidino-phosphiren-2-ylid, $E_{\text {rel }}=166$ $\mathrm{kJ} \mathrm{mol}^{-1}$ ) are neglected in this study

allyl structure is preferred over the three-membered ring for phosphanides.[7] This raises the question whether the bicyclic form is really the best structure for $\mathrm{HP}_{4}-$. Therefore in the following, relative energies for $\mathrm{HP}_{4} \mathrm{R}$ structures (with R $=$ negative charge, and Na ) are presented together with their MO analysis. The discussion places these results in the context of similar investigations in $\mathrm{HP}_{4} \mathrm{R}$ systems with $\mathrm{R}=\mathrm{H},[8,9]$ and Li [4] as substituent. The sodium ion pair structures are considered to obtain an impression of the counterion effect on the structural preference and the NMR chemical shifts of the $\mathrm{HP}_{4}{ }^{-}$isomers. For a comprehensive set of phosphanides including the cyclo- $\mathrm{P}_{3}\left(\mathrm{CH}_{2}\right)^{-}$, which is isovalent to $\mathbf{1}$, their geometries and computed chemical shifts are presented. These provide an estimate for the agreement between experimental $\delta^{31} \mathrm{P}$ and the corresponding values from MP2/NMR calculations, which neglect the solvent as well as the counterion effect. The experimental $\delta^{31} \mathrm{P}\left(\mathrm{HP}_{4}(\mathrm{Na} / \mathrm{K})\right.$, DME) are reinterpreted based on these results.

## Computational details

The geometries of $\mathrm{HP}_{4}^{-}, \mathrm{P}_{3}\left(\mathrm{CH}_{2}\right)^{-}$and related molecules were optimized at the MP2(fc) $/ 6-31+G(d)$ level. The basis set includes diffuse functions, which are required for sufficient description of anionic molecules. The $\mathrm{HP}_{4}{ }^{-}$geometries are presented in Figure 2, whereas details of the $\mathrm{P}_{3}\left(\mathrm{CH}_{2}\right)^{-}$and $\mathrm{HP}_{4} \mathrm{Na}$ calculations are in the supplementary material. Throughout this paper, bond lengths are given in Ångstrøm, bond angles in degrees, and relative energies in $\mathrm{kJ} \mathrm{mol}^{-1}$. Relative energies are with respect to $\mathbf{1}$ for the $\mathrm{HP}_{4}{ }^{-}$anions and with respect to $\mathbf{1 1}$ for the $\mathrm{HP}_{4} \mathrm{Na}$ geometries. The ${ }^{31} \mathrm{P}$ NMR chemical shifts, $\delta_{\text {calc }}{ }^{31} \mathrm{P}$, were computed at the GIAO/ MP2 /6-311+G(d), GIAO/MP2 /6-31+G(d) and for comparison also at GIAO/B3LYP $/ 6-31+\mathrm{G}(\mathrm{d})$ with $\mathrm{PH}_{3}$ in $6-31 \mathrm{G}(\mathrm{d}, \mathrm{p})$ geometry as theoretical reference. All calculations including calculation of the Wiberg bond index [10] were carried out using the GAUSSIAN 98 [11] set of programs.

## Results and discussion

Minimum structures of $\mathrm{HP}_{4}{ }^{-}$and $\mathrm{CH}_{2} \mathrm{P}_{3}{ }^{-}$
For $\mathrm{HP}_{4}{ }^{-}$only one "Baudler Structure" [12], $\mathbf{2}$ in this study, exists. Nevertheless, several other structures are minima on this energy hypersurface with $\mathbf{1}$ as the lowest energy isomer $\left(\mathrm{E}_{\mathrm{rel}}(\mathbf{2})=23.3 \mathrm{~kJ} \mathrm{~mol}^{-1}\right)$. While the optimized geometries of $\mathbf{1}$ to $\mathbf{3}$ are shown in Figure 2, the linear H-PPPP- minimum with s-cis conformation $\left(\mathrm{E}_{\text {rel }}=119 \mathrm{~kJ} \mathrm{~mol}^{-1}\right)$ and the phosphinidine structure (cyclo-(P)(PH)(P-P:) ${ }^{-}, \mathrm{E}_{\mathrm{rel}}=166 \mathrm{~kJ}$ $\mathrm{mol}^{-1}$ ) are neglected due to their high energies. In all structures considered the phosphorus atoms can be classified in three types: $\mathrm{P}_{\mathrm{A}}$, the formally anionic phosphorus, $\mathrm{P}_{\mathrm{B}}$ and $\mathrm{P}_{\mathrm{B}}$, two symmetry equivalent phosphorus atoms, and $\mathrm{P}_{\mathrm{C}}$, a $\sigma^{3}-\mathrm{P}$. The allyl conjugation of the $P_{B}-P_{A}-P_{B}$, fragment in $\mathbf{1}$ and $\mathbf{4}$ is characterized by $\mathrm{P}_{\mathrm{A}}-\mathrm{P}_{\mathrm{B}}$ bond lengths of 2.135 and $2.119 \AA$, respectively, which are similar to that in the acyclic H-PPP-$\mathrm{H}^{-}$anion [7] (2.096 $\AA$ at MP2/6-31+G(d) and 2.09(2) $\AA$ in the crystal structure of $\left[{ }^{1} \mathrm{Bu}_{3} \mathrm{Si}-\mathrm{PPP}-\mathrm{Si}^{\mathrm{t}} \mathrm{Bu}_{3} \cdot \mathrm{Na}(\mathrm{THF})_{4}\right)$. While reducing the $P_{B}-P_{A}-P_{B}$, bond angle in the allyl system from $108.2^{\circ}$ of the acyclic compound [7] to $96.8^{\circ}$ in $\mathbf{1}$ induces an elongation of the $\mathrm{P}_{\mathrm{A}}-\mathrm{P}_{\mathrm{B}}$ bond by $0.04 \AA$, stronger bending in $4\left(\mathrm{P}_{\mathrm{B}}-\mathrm{P}_{A}-\mathrm{P}_{\mathrm{B}},=88.6^{\circ}\right)$ means less lengthening of the $\mathrm{P}_{\mathrm{A}}-\mathrm{P}_{\mathrm{B}}(\Delta$ $=0.02 \mathrm{~A})$. From 1 to $\mathbf{2}$, the $\mathrm{P}_{\mathrm{A}}-\mathrm{P}_{\mathrm{B}}$ bond changes its character from a partial $\pi$-bond to a single bond. Due to the $\pi$ donor character of the occupied p-AO at $\mathrm{P}_{\mathrm{A}}$, which is orthogonal to the $\mathrm{P}_{\mathrm{A}} \mathrm{P}_{\mathrm{B}} \mathrm{P}_{\mathrm{B}}$, plane, the $\mathrm{P}_{\mathrm{C}}-\mathrm{P}_{\mathrm{B}}$ and $\mathrm{P}_{\mathrm{C}}-\mathrm{P}_{\mathrm{B}}$, bond are elongated while the $P_{A}-P_{B}$ and $P_{A}-P_{B}$, bonds shrink compared to bicyclo $\mathrm{H}_{2} \mathrm{P}_{4}-\left(\mathrm{HP}-\mathrm{P}=2.229 \AA\right.$ in the exo, exo isomer). For $\mathrm{HP}_{4}{ }^{-}$the non-Baudler structure $\mathbf{1}$ is preferred even more over $\mathbf{2}$ than for $\mathrm{P}_{3}\left(\mathrm{CH}_{2}\right)^{-}$with $\mathrm{E}_{\text {rel }}(\mathbf{5})=10.6 \mathrm{~kJ} \mathrm{~mol}^{-1}$ (relative to 4). An impression of the location of the negative molecular charge can be obtained from the Mulliken charges, $\mathrm{q}_{\mathrm{M}}$. As expected for an allylic delocalization, the anionic charge of $\mathbf{1}$ is not localized at $\mathrm{P}_{\mathrm{A}}$ since the HOMO has two nodal planes at $\mathrm{P}_{\mathrm{A}}$ $\left(q_{M}\left(P_{A}\right)\right.$ is only -0.08 , while $q_{M}\left(P_{B}\right)$ is -0.44$)$. In 3 the negative molecular charge should be located in the exocyclic phosphanido group. Nevertheless, $\mathrm{q}_{\mathrm{M}}\left(\mathrm{P}_{\mathrm{A}}\right)$ and $\mathrm{q}_{\mathrm{M}}(\mathrm{H})$ are to-

Figure 2 MP2 $\left(f_{c}\right) / 6-31+G(d)$ optimized geometries of the $\mathrm{HP}_{4}-$ and $\mathrm{CH}_{2} \mathrm{P}_{3}^{-}$anion structures considered. Bond length in $\AA$, bond angles in degree

$$
\begin{gathered}
\mathrm{P}_{\mathrm{B}}-\mathrm{P}_{\mathrm{B}^{\prime}}=3.193 \\
\mathrm{t}\left(\mathrm{P}_{\mathrm{C}} \mathrm{P}_{\mathrm{B}^{\prime}} \mathrm{P}_{\mathrm{B}} \mathrm{P}_{\mathrm{A}}\right)=-160.3
\end{gathered}
$$



1 Cs

$\mathrm{t}\left(\mathrm{P}_{\mathrm{C}} \mathrm{P}_{\mathrm{B}} \mathrm{P}_{\mathrm{B}} \mathrm{P}_{\mathrm{A}}\right)=$ 2endo $\mathrm{C}_{\mathrm{s}}$.
111.9
$\mathfrak{t}\left(\mathrm{P}_{\mathrm{C}} \mathrm{P}_{\mathrm{B}}, \mathrm{P}_{\mathrm{B}} \mathrm{P}_{\mathrm{A}}\right)=$ 2exo $\mathrm{C}_{\mathrm{s}}$ 103.3


gether only -0.53 electron charges. A similar distribution of the anionic charge between $\mathrm{P}_{\mathrm{A}}$ and the remaining molecule occurs in 2: $\mathrm{q}_{\mathrm{M}}\left(\mathrm{P}_{\mathrm{A}}\right.$, 2exo $)=-0.60, \mathrm{q}_{\mathrm{M}}\left(\mathrm{P}_{\mathrm{A}}\right.$, 2endo $)=-0.63$. The charge delocalization is reflected by shortened $P_{A}-P_{B}$ and widened $\mathrm{P}_{\mathrm{B}}-\mathrm{P}_{\mathrm{C}}$ bonds in $\mathbf{2}$ compared to bicyclo $\mathrm{H}_{2} \mathrm{P}_{4}$ (HP-P $=$ $2.229 \AA$ in the exo,exo isomer). The donor character of p$\mathrm{AO}\left(\mathrm{P}_{\mathrm{A}}\right)$ towards $\mathrm{P}_{\mathrm{C}}$ in the bicycle 2 is small $\left(\mathrm{WBI}\left(\mathrm{P}_{\mathrm{A}}-\mathrm{P}_{\mathrm{C}}\right)<\right.$ 0.2 ). While the partial $\mathrm{P}_{\mathrm{A}}-\mathrm{P}_{\mathrm{C}}$ bonding reflects the descent from the $P_{4}$ cage, the cluster character should vanish in $\mathbf{3}$ since
two bonds of white phosphorus are opened and only one deltahedron remains.

A P-P double bond characterizes 3, phosphinidinophosphirene, with $\mathrm{E}_{\text {rel }}$ of 30.8 and $40.1 \mathrm{~kJ} \mathrm{~mol}^{-1}$. For the parent cyclo- $(\mathrm{PH})(\mathrm{P})_{2}$ the double bond length was calculated to be 1.981 [13] at RHF/DZP and is $2.033 \AA$ at the level of this study. The corresponding $P_{B}-P_{B}$, bond in $\mathbf{3}$ is distinctly longer (2.122 and $2.113 \AA$, Figure 2) due to the negative hyperconjugation of the $\mathrm{p}-\mathrm{AO}\left(\mathrm{P}_{\mathrm{A}}\right)$ which matches the sym-

Table 1 Experimental and GIAO/MP2(fc) /6-311+G(d)//MP2(fc)/6-31+G(d) calculated [a] ${ }^{31} P$ NMR chemical shifts of compounds [b] with anionic $P_{3}$ moiety (relative energies [c] of $\mathrm{HP}_{4}^{-}$in $\mathrm{kJ} \mathrm{mol}{ }^{-1}$ )

| Structure | $\mathbf{E}_{\text {rel }}[\mathrm{c}]$ | $\mathbf{P}_{\text {A }}[\mathrm{b}]$ | $\mathrm{P}_{\mathrm{B}}$ [b] | $\mathrm{P}_{\mathrm{C}}[\mathrm{b}]$ |
| :---: | :---: | :---: | :---: | :---: |
| $\left[\mathrm{P}(\mathrm{PR})_{2}\right](\mathrm{Na}, 4 \mathrm{THF})$,exp. [d] | - | 732.5 | 212.5 | - |
| [P(PR) $2^{2}$-, alltrans [d] | - | 595 | 168 | - |
| [cyclo-P(PR) $2^{\text {] }}$-,trans [d] | - | -275 | -255 | - |
| [cyclo-P(PR) $2^{\text {] }}$ - , cis [d] | - | -251 | -281 | - |
| $\mathrm{HP}_{4}(\mathrm{Na} / \mathrm{K}, \mathrm{DME})$, exp. [e] | - | +71.3 | -355.1 | -329.5 |
| $\mathrm{HP}_{4}{ }^{-}$, 1 | 0.0 | 517 | 424 | 50 |
| $\mathrm{HP}_{4}^{-}, 2$ endo | 24.7 | 221 | -322 | 350 |
| $\mathrm{HP}_{4}^{-}$,2exo | 23.3 | -16 | -360 | -120 |
| $\mathrm{HP}_{4}{ }^{-}$, 3endo | 41.1 | 377 | -268 | -261 |
| $\mathrm{HP}_{4}^{-}$, 3exo | 30.8 | -78 | -247 | -286 |
| $\mathrm{P}_{3}(\mathrm{CH})_{2}{ }^{-}$, exp. [f] | - | 272.0 | 262.9 | - |
| cyclo-1,2,3-P ${ }_{3}(\mathrm{CH})_{2}{ }^{-}, C_{2 v}$ | 0.0 | $279{ }^{\text {e }}$ | $264{ }^{\text {e }}$ | - |
| bicyclo- $\mathrm{P}_{3}(\mathrm{CH})_{2}{ }^{-} \mathrm{C}_{s}$ | 220.0 | $301{ }^{\text {g }}$ | $-170^{\text {g }}$ | - |
| cyclo-1,2,3-P ${ }_{3}\left(\mathrm{CH}_{2}\right)^{-}, C_{2 v}$ | 0.0 | 611 | 450 | - |
| bicyclo- $\mathrm{P}_{3}\left(\mathrm{CH}_{2}\right)^{-}, C_{s}$ | 10.6 | 23 | -355 | - |

[a] Chemical shifts calculated using $\mathrm{PH}_{3}$ in MP2/6-31G(d,p) geometry as theoretical reference with $?^{31} P=-240$ and $\sigma^{31} P$ $=616.8 \mathrm{ppm}$
[b] $P_{A}$ is dicoordinate and occurs once; $P_{B}$ occurs twice and is attached to $P_{A} ; P_{C}$ is tricoordinate and occurs once [c] At MP2(fc)/6-31+G(d) the total energy of 1 is -1363.92945 Hartree
[d] The substituent $R$ is $H$ in the computed molecules and ${ }^{t} B u_{3} S i-P$ in the experiment.[18] [e] Reference 5. [f] Reference 14
[g] Chemical shifts calculated at GIAO/MP2/6-311G(d) using $\mathrm{PH}_{3}$ in $M P 2 / 6-31 G(d, p)$ geometry as theoretical reference with $\sigma^{31} P=616.9 \mathrm{ppm}$
metry of the $\pi^{*}\left(\mathrm{P}_{\mathrm{B}}-\mathrm{P}_{\mathrm{B}},\right)$ group orbital. This is supported by calculation of the transition structure for rotation around the $P_{A}-P_{C}$ bond in which the double bond length is about as long as in the parent $\mathrm{HP}_{3}(2.033 \AA)$. The consequences of the remarkable $\mathrm{P}_{\mathrm{A}}{ }^{-} \pi^{*}\left(\mathrm{P}_{\mathrm{B}}-\mathrm{P}_{\mathrm{B}}\right.$ ) conjugation for the predicted ${ }^{31} \mathrm{P}$ NMR signals are discussed in the following section together with a scan over $\delta^{31} \mathrm{P}$ of different model phosphanides.

## NMR chemical shifts

For the $\mathrm{P}_{4} \mathrm{H}^{-}$structures considered the high level ab inito calculations of the phosphorus NMR chemical shifts, $\delta_{\text {calc }}{ }^{31} \mathrm{P}$, of all P atoms are presented in Table 1. After comparing the characteristic $\delta^{31} \mathrm{P}$ of $\mathrm{P}_{\mathrm{A}}$ in $\mathbf{1 - 5}$ with the $\sigma^{2}-\mathrm{P}$ in various phosphid anions (Table 2) the effect of molecular motion is considered. At last, $\delta_{\text {calc }}{ }^{31} \mathrm{P}$ for the $\mathrm{P}_{4} \mathrm{HNa}$ complexes at a practicable level of theory are considered to estimate the effect of the sodium cation (Table 3).

From Table 1 it becomes clear that none of the sets of calculated chemical shifts for single structures $\left(\delta^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{A}}, \mathrm{i}\right)\right.$, $\delta^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{B}}, \mathrm{i}\right)$, and $\delta^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{C}}, \mathrm{i}\right)$ values for $\mathrm{i}=1,2$ endo, 2exo, 3endo, and 3exo) alone matches the experimental data set. While $\mathrm{P}_{\mathrm{C}}$ in structure $\mathbf{1}$ comprising a triphosphaallyl moiety $\left(\delta_{\text {calc }}{ }^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{C}}\right.\right.$, $\mathbf{1})=50 \mathrm{ppm}$, Table 1) has about the chemical shift assigned to the anionic phosphorus in an assumed bicyclic structure, the $\delta_{\text {calc }}{ }^{31} \mathrm{P}$ of the other nuclei are more than 700 ppm
downfield from the remaining $\delta_{\text {calc }}{ }^{31} \mathrm{P}$. For the bicyclic $\mathrm{P}_{4} \mathrm{H}^{-}$ structures, 2endo and 2exo, the $\delta_{\text {calc }}{ }^{31} \mathrm{P}$ values for the two $\mathrm{P}_{\mathrm{B}}$ nuclei agree reasonably well with the experimental $P_{B}$ value (deviations of 33 for 2endo and -5 for 2exo). In disfavor of these structures, the $\delta_{\text {calc }}{ }^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{C}}, \boldsymbol{2}\right)$ differ by 210 and 680 ppm from $\delta_{\text {exp }}{ }^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{C}}\right)$. The experimental $\delta^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{A}}, \boldsymbol{2}\right)$ is in the middle between the two corresponding calculated values. Nevertheless, endo/exo isomerization is not likely to be fast enough to provide an averaged signal for the bicyclic structures. In contrast, for the rotamers 3endo and 3exo averaging is likely at room temperature (rotational barrier: $53 \mathrm{~kJ} \mathrm{~mol}^{-1}$ at MP2(fc)/6-31+G(d)level) and thereby provides a $\delta_{\text {calc,av }}{ }^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{A}}\right)$ close to the experiment. For the two $\mathrm{P}_{\mathrm{B}}$ and the one $P_{C}$ of $\mathbf{3}$ the calculated NMR shifts deviate from the corresponding $\delta_{\text {exp }}{ }^{31} \mathrm{P}$ by less than 105 ppm . In conclusion, differentiation between the allylic, $\mathbf{1}$, and the other cyclic isomers based on the $\delta_{\text {calc }}{ }^{31} \mathrm{P}$ values appears to be justified even if the effect of a coordinated sodium cation is neglected (the $\delta^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{B}}\right)$ at GIAO/MP2/6-31+G(d) for the $[1 * \mathrm{Na}]$ complexes differ from those of $\mathbf{1}$ by 47 for $\mathbf{6}$ and zero for $\mathbf{7}$; while $\delta^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{B}}\right.$, 1) > 300 is distinctly different to the $\delta^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{B}}, 2\right)$ and $\delta^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{B}}\right.$, 3) $<-200 \mathrm{ppm}$ ). Nevertheless, for a confirmative assignment of the experimental $\delta^{31} \mathrm{P}$ to either 2 or $\mathbf{3}$ the effect of $\mathrm{Na}^{+}$ should be considered. Comparison of the experimentally known data corresponding to the anions $\mathrm{PH}_{2}^{-}, \mathrm{P}\left(\mathrm{SiH}_{3}\right)_{2}^{-}$, and $\mathrm{P}\left(\mathrm{PH}_{2}\right)\left(\mathrm{SiH}_{3}\right)^{-}$with the $\delta_{\text {calc }}{ }^{31} \mathrm{P}$ in Table 2 gives the impression that the sodium cation changes $\delta^{31} \mathrm{P}$ towards lower field.

Table 2 Calculated [a] NMR chemical shifts [b,c] of the $\sigma^{2}-P$ with the $\alpha$ substituents [d] $X$ an $Y$ in acyclic and cyclic structures comprising the phosphanide moiety

| Molecule | X | Y | $\begin{gathered} \delta^{31} \mathbf{P} \\ \text { MP2 }[\mathrm{b}] \end{gathered}$ | $\begin{gathered} \delta^{31} \mathbf{P} \\ \text { DFT }[\mathrm{c}] \end{gathered}$ | $\delta_{\text {exp }}{ }^{31} \mathrm{P}[\mathrm{e}-\mathrm{m}]$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{PH}_{2}{ }^{-}$ | H | H | -358 | -350 | -283 [e] |
| PH-Me ${ }^{-}$ | $\mathrm{CH}_{3}$ | H | -157 | -128 | - |
| $\mathrm{PMe}_{2}{ }^{-}$ | $\mathrm{CH}_{3}$ | $\mathrm{CH}_{3}$ | 17 | 53 | - |
| $\mathrm{PH}-\mathrm{SiH}_{3}{ }^{-}$ | $\mathrm{SiH}_{3}$ | H | -361 | -338 | -335.4 [f] |
| $\mathrm{P}\left(\mathrm{SiH}_{3}\right)_{2}{ }^{-}$ | $\mathrm{SiH}_{3}$ | $\mathrm{SiH}_{3}$ | -399 | -380 | $-300 \pm 5[\mathrm{~g}]$ |
| $\mathrm{PH}-\mathrm{PH}_{2}{ }^{-}$ | $\mathrm{PH}_{2}$ | H | -168 | -151 | 17.4 [h] |
| $\mathrm{P}\left(\mathrm{PH}_{2}\right)\left(\mathrm{SiH}_{3}\right)^{-}$ | $\mathrm{PH}_{2}$ | $\mathrm{SiH}_{3}$ | -319 | -288 | -176.8 [i] |
| $\mathrm{P}\left(\mathrm{PH}_{2}\right)_{2}{ }^{-}$ | $\mathrm{PH}_{2}$ | $\mathrm{PH}_{2}$ | -209 | -177 | 732.5 |
| $\mathrm{P}(\mathrm{PH})_{2}{ }^{-}$ | PH | PH | 501 | 685 | 732.5 [j] |
| cyclo-P(PH) ${ }_{2}{ }^{-}$ | PHR [d] | PHR [d] | -285 | -236 | - [j] |
| 2 exo bicyclo- $\mathrm{HP}_{4}^{-}$ | PRR' [d] | PRR' [d] | -48 | -17 | - |
| 2endo bicyclo- $\mathrm{HP}_{4}{ }^{-}$ | PRR' [d] | PRR' [d] | 166 | 200 | - |
| 1 cyclo- $\mathrm{HP}_{4}^{-}$ | PR [d] | PR [d] | 426 | 668 | - |
| 4 cyclo- $\mathrm{P}_{3}\left(\mathrm{CH}_{2}\right)^{-}$ | PR [d] | PR [d] | 516 | 729 | - [k] |
| 5 bicyclo- $\mathrm{P}_{3}\left(\mathrm{CH}_{2}\right)^{-}$ | PR [d] | PR [d] | -10 | 37 | - [k] |
| cyclo- $\mathrm{P}_{5}{ }^{-}$ | PR [d] | PR [d] | - [b] | 495 | 467.2 [1] |
| cyclo-P(CH) ${ }^{-}$ | $\mathrm{CH}_{2} \mathrm{R}$ [d] | $\mathrm{CH}_{2} \mathrm{R}$ [d] | 51 | 54 | 77.2 [m] |
| cyclo- $\mathrm{P}_{3}(\mathrm{CH})_{2}{ }^{-}$ | PR [d] | PR [d] | 237 | 330 | 272.0 [k] |

[a] Based on RMP2(fc)/6-31+G(d) optimized geometries [b] GIAO /MP2 /6-31 $+G(d)$ calculated magnetic shieldings transformed to $\delta^{31} P$ with the theoretical reference $\sigma^{31} P\left(\mathrm{PH}_{3}\right.$ in MP2/6-31G(d,p) geometry) $=648.4$ ppm. The $P_{5}^{-}$could not be calculated due to computational limitations
[c] GIAO/B3LYP/6-31 $+G(d)$ calculated magnetic shieldings transformed to $\delta^{31} P$ with the theoretical reference $\sigma^{31} P\left(\mathrm{PH}_{3}\right.$ in MP2/6-31G(d,p) geometry) $=589.0 \mathrm{ppm}$
[d] Substituent $R, R$ 'are endocyclic $\sigma^{2}$ or $\sigma^{3}$ phosphorus
[e] Value for $\mathrm{NaPH}_{2}{ }^{*}$ monoglym [16]
$[f]$ Values for ${ }^{t} \mathrm{Bu} u_{3} \mathrm{Si}-\mathrm{PH}$ anion with $\mathrm{Li}^{+}$as counterion in THF solution (2 THF directly coordinate to the cation); for the corresponding sodium solution $\delta^{31} P=-327.7$ [17]
[g] Values for $\left(\mathrm{Me}^{3} \mathrm{Si}\right)_{2} \mathrm{P}$ with $\mathrm{Li}^{+}$as counterion and various solvents [18]
[h] In the terminal groups of [ $\left.n-(P P h)_{3}\right]^{2-}\left(K^{+}\right)_{2}$ [19]
[i] Value for ${ }^{t} \mathrm{Bu}_{3} \mathrm{Si}-\mathrm{P}^{-}-\left(\mathrm{P}_{3} R_{2}\right)$ with $\mathrm{Na}^{+}$as counterion [17]
[j] Value for ( $\left.{ }^{t} \mathrm{Bu} u_{3} \mathrm{Si}-\mathrm{P}\right)_{2} \mathrm{P}^{-}$with $\mathrm{Na}^{+}$as counterion (4 THF directly coordinate to $\mathrm{Na}^{+}$) [17]
[k] Value for cyclo- $(\mathrm{P})_{3}(\mathrm{CH})_{2}{ }^{-}$. The early assignment to $\mathrm{CH}_{2} \mathrm{P}_{3}{ }^{-}$was refuted [14]
[l] Value for $P_{5}(N a,[18]$ crown-6,THF] solution and 470.2 ppm for the reaction solution [20]
[m] Value for $\mathrm{C}_{4} \mathrm{H}_{4} \mathrm{P}^{-}$with $\mathrm{Li}^{+}$as counterion in THF solution [6]
lated from first substituent effects. The deviation of $\delta^{31} \mathrm{P}$ for $\mathrm{R}_{2} \mathrm{P}^{-}$is probably partially due to the $\mathrm{Na}^{+}$coordinating to the anion in solution. Since experimental values are all at lower field ( +26 with $\mathrm{R}=\mathrm{H}, \mathrm{R}{ }^{\prime}=\mathrm{SiH}_{3} ;+75$ with $\mathrm{R}=\mathrm{R}^{\prime}=\mathrm{H} ;+99$ ppm with $\mathrm{R}=\mathrm{R}^{\prime}=\mathrm{SiH}_{3}$ ), the sodium effect can be expected to reduce the magnetic shielding of phosphorus. For all saturated substituents the GIAO/B3LYP chemical shifts of RR'Pare in reasonable agreement with the corresponding GIAO/ MP2 values (B3LYP shifts deviate by +8 to +36 ppm from the MP2 results both obtained with the $6-31+\mathrm{G}(\mathrm{d})$ basis set). In contrast, for the unsaturated substituents (cf. values in the lower part of Table 2) the GIAO/B3LYP chemical shifts show larger deviations from the GIAO/MP2 data. At both levels the reported $\delta^{31} \mathrm{P}$ for the phospholide, cyclo- $(\mathrm{CH})_{4} \mathrm{P}$, is in reasonable agreement with $\delta_{\text {calc }}{ }^{31} \mathrm{P}$ ( 26 ppm deviation at GIAO/ MP2 and 29 ppm at GIAO/B3LYP). Coincidentally, the $\delta^{31} \mathrm{P}$ of $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{P}^{-}$and the phospholide are quite similar. In case of

Table 3 GIAO/MP2 $(f c) / 6-31+G(d) / / M P 2(f c) / 6-31+G(d)$ calculated [a] ${ }^{31} P$ NMR chemical shifts and relative energies [b] (in $\mathrm{kJ} \mathrm{mol}{ }^{-1}$ ) of $\mathrm{HP}_{4}^{-}$anions and $\mathrm{HP}_{4} \mathrm{Na}$ complexes [c]

| Structure [b] | $\mathbf{E}_{\text {rel }}[\mathrm{b}]$ | $\mathbf{P}_{\mathrm{A}}$ [c] | $\mathrm{P}_{\mathrm{B}}$ [c] | $\mathrm{P}_{\mathrm{C}}[\mathrm{c}]$ |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{HP}_{4}{ }^{-}, 1$ | 0.0 | 426 | 350 | 15 |
| $\mathrm{HP}_{4}^{-}$, 2endo | 24.7 | 166 | -318 | 303 |
| $\mathrm{HP}_{4}^{-}$, 2exo | 23.3 | -48 | -350 | -130 |
| $\mathrm{HP}_{4}^{-}$, 3endo | 41.1 | 319 | -288 | -263 |
| $\mathrm{HP}_{4}^{-}$, 3exo | 30.8 | -98 | -259 | -280 |
| 6, $C_{s}$ | 16.7 | 407 | 397 | 17 |
| 7, $C_{s}$ | 12.9 | 320 | 350 | 2 |
| 8, $C_{s}$ | 30.2 | 89 | -333 | 330 |
| 9, $C_{s}$ [d] | 46.5 | 128 | -308 | 319 |
| 10, $C_{s}$ | 117.1 | 241 | -286 | 172 |
| 11, $C_{s}$ | 0.0 | -120 | -364 | -141 |
| 12, $C_{s}$ | 26.2 | -91 | -367 | -63 |
| 13, $C_{s}$ | 89.2 | 438 | -204 | -324 |
| 14, $C_{s}$ | 72.1 | -20 | -189 | -317 |
| 15, $C_{1}{ }^{\text {a }}$ | 65.9 | 157 | - [e] | -252 |
| 16, $C_{s}$ | 15.4 | -35 | -257 | -311 |
| exp. [f], $C_{s}$ | - | 71 | -355 | -330 |

[a] Chemical shifts calculated using $\mathrm{PH}_{3}$ in MP2/6-31G(d,p) geometry as theoretical reference with $\delta^{31} P=-240$ and $\sigma^{31} P$ $=648.4 \mathrm{ppm}$
[b] Point groups of the geometry obtained without symmetry constraint. The total energy of 1 is -1363.92945 Hartree. The total energy of 11 is -1525.78079 Hartree
[c] $P_{A}$ is the anionic phosphorus (occurs once); $P_{B}$ occurs
twice and is attached to $P_{A} ; P_{C}$ is tricoordinate and attached to hydrogen.
[d] In the shallow potential area the $\mathrm{C}_{\mathrm{s}}$ structure has one imaginary vibration mode with only il5 $\mathrm{cm}^{-1}$.
[e] For the $P_{B}$ attached to $N a^{+} \delta^{3 l} P$ is -4 and for the other $P_{B}$ $\delta^{31} P$ is -42 ppm
[f] Double intensity reported for $P_{B}$. $[5]$
shift calculated for the $\sigma^{2}-\mathrm{P}$ in the phosphirene ring of 3endo and 3exo are related to a much more complex molecular orbital, MO, structure. Since simplified depictions of the valence MOs of phosphorus with 2 p type AOs instead of 3 p AOs (e.g. Figure 1 in an article [8] about the $\mathrm{P}_{4} \mathrm{H}_{2} \mathrm{MOs}$ ) give correct symmetries but may present a misleading overlap, the MOs in Figure 3 are presented as 3D objects in the supplementary material. The MOs of the bicyclic structure as well as the phosphirene derivative can be constructed based on the $\mathrm{P}_{\mathrm{B}}-\mathrm{P}_{\mathrm{B}}$, fragment with two orthogonal $\pi$ bond group orbitals (relative orientations of the $\pi$ bonds specified in Figure $3 ; \mathrm{P}_{\mathrm{A}}-\mathrm{P}_{\mathrm{C}}$ parallel X axis, $\mathrm{P}_{\mathrm{B}}-\mathrm{P}_{\mathrm{B}}$, parallel Y axis). As in the previous $\mathrm{P}_{4} \mathrm{H}_{2}$ study [8] the group orbitals of PH and $\mathrm{P}^{-}$can be added to this group to form the bicyclic structures $\mathrm{P}_{4} \mathrm{H}_{2}$, 2endo and 2exo. The phosphinophosphirane $\mathbf{3}$ is obtained by adding the bare end of the anionic P- $\mathrm{PH}^{-}$fragment to $\mathrm{P}_{\mathrm{B}} \mathrm{P}_{\mathrm{B}^{\prime}}$. The HOMO of $\mathrm{P}_{4} \mathrm{H}_{2}$ (exo,exo; $\mathrm{a}_{1}$ in $C_{2 v}$ ) as well as the 29 th MOs (HOMO-3) of the $\mathrm{P}_{4} \mathrm{H}^{-}$isomers 2endo and 2exo are not only characterized by the $\pi$ bonding $3 p_{z} \mathrm{AOs}$ at $\mathrm{P}_{\mathrm{B}}$ and $\mathrm{P}_{\mathrm{B}}$, but also comprise $3 p_{z}$ AOs at $\mathrm{P}_{\mathrm{A}}$ and $\mathrm{P}_{\mathrm{C}}\left(\mathrm{P}_{\mathrm{A}^{\prime}}\right.$, respectively). At the MP2 level the MNDO order [8] of symmetry orbitals in tetraphosphabicyclo[1.1.0]butane is only confirmed for the HOMO and HOMO-1 (Figure 3). The $4 \mathrm{a}_{1} \mathrm{MO}$ [8] with $\sigma\left(\mathrm{P}_{\mathrm{B}} \mathrm{P}_{\mathrm{B}}\right.$ ) character is not HOMO-2 but HOMO-4 with a $b_{2}$ $\left(\mathrm{Lp}_{\mathrm{z}}\right.$ at PH groups, antibonding) and a MO with $\mathrm{a}_{2}$ symmetry


Figure $3 M O$ energies in eV at $M P 2(f c) / 6-31+G(d) / /$ $M P 2(f c) / 6-31+G(d)$ of the $\mathrm{HP}_{4}^{-}$anions 1 - 3
( $\pi^{*}\left(\mathrm{P}_{\mathrm{B}} \mathrm{P}_{\mathrm{B}}\right.$ ) combined bonding with $3 p_{y} \mathrm{AOs}$ at the PH groups) forming HOMO-3 and HOMO-2.

In contrast to bicyclic $\mathrm{P}_{4} \mathrm{H}_{2}$, the bicyclic $\mathrm{P}_{4} \mathrm{H}^{-}$isomers 2endo and 2exo have no $\pi\left(\mathrm{P}_{\mathrm{B}} \mathrm{P}_{\mathrm{B}}\right.$, ) character of their HOMOs but are primarily a 3 p AO at $\mathrm{P}_{\mathrm{A}}$. Despite the negative charge of 2 and different MOs, the chemical shifts of $P_{B}$ are predicted to be quite similar to those of the bridgehead phosphorus in exo,exo $\mathrm{P}_{4} \mathrm{H}_{2}\left(\delta_{\text {calc }}{ }^{31} \mathrm{P}=-378 \mathrm{ppm}\right.$ at GIAO/MP2 / $6-311+G(d)$ level). As the folding angle of the triangles of the bicycle increases from $103.6^{\circ}$ to $113.5^{\circ}$ (endo,exo to endo,endo $\mathrm{P}_{4} \mathrm{H}_{2}$ ) and from $103.3^{\circ}$ to $111.9^{\circ}$ (2exo to 3endo) the $\delta^{31} \mathrm{P}_{\text {bridgehead }}$ changes by about 45 ppm downfield in both structures. In bicyclo $\mathrm{P}_{4} \mathrm{H}_{2}$ as well as in 2 the $\delta_{\text {calc }}{ }^{31} \mathrm{P}$ of the PH groups are more sensitive to the endo or exo orientation of the PH bond than the bridgehead phosphorus. Remarkably, the endolexo effect is larger in $2\left(\delta^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{C}}, \mathbf{2 e n d o}\right)\right.$ is

470 ppm downfield relative to $\delta^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{C}}\right.$, 2exo, 440 ppm at the GIAO/MP2/6-31+G(d) level) where only one P-H bond changes the orientation, than between the exo,exo and the endo,endo conformer of bicyclo $\mathrm{P}_{4} \mathrm{H}_{2}\left(\delta^{31} \mathrm{P}(\mathrm{PH} ;\right.$ exo,exo $)=-$ $227, \delta^{31} \mathrm{P}(\mathrm{PH} ;$ endo, endo $)=22$, at the GIAO/MP2 $/ 6-31+\mathrm{G}(\mathrm{d})$ level). An indicator for the difference between these otherwise quite similar structures is the Wiberg Bond index, WBI, of the P-P bond of tetrahedral $\mathrm{P}_{4}$, which is opened in 2 ; the $\operatorname{WBI}\left(\mathrm{P}_{\mathrm{A}}-\mathrm{P}_{\mathrm{C}}, 2\right)$ is 0.18 , while it is only 0.03 for $\mathrm{P}_{\mathrm{C}}-\mathrm{P}_{\mathrm{C}}$, in exo, exo $\mathrm{P}_{4} \mathrm{H}_{2}$. Which MOs reflect this rudimental bond of tetrahedral $\mathrm{P}_{4}$ in the different isomers, endo and exo? Since the $\mathrm{P}-\mathrm{H}$ bond, which changes its orientation, lies in the mirror plane of the $C_{s}$ symmetric molecules 2, these MOs with a" character should show less differences between endo and exo than those of a' symmetry character (Figure 3) with electron density in the plane comprising $\mathrm{P}_{\mathrm{A}}, \mathrm{P}_{\mathrm{C}}$ and H . While the order of the symmetry MOs are the same for 2endo and for 2exo, the MO energies differ: ( $\varepsilon(\mathbf{2 e x o})-\boldsymbol{\varepsilon}(\mathbf{2 e n d o})$ in eV : 0.09 for 21a', -0.22 for 10 a ", 0.22 for 20a', and 0.16 for $9 a^{\prime \prime}$ ). In MO 10a' the endo/exo difference is most pronounced: at the $\mathrm{P}_{\mathrm{A}} \mathrm{P}_{\mathrm{B}} \mathrm{P}_{\mathrm{B}}$, moiety is a combination of $\pi$ bonding $3 p_{z}\left(\mathrm{P}_{\mathrm{B}}\right)$, $3 p_{z}\left(\mathrm{P}_{\mathrm{B}},\right)$ with a $3 p_{x} \mathrm{AO}$ at $\mathrm{P}_{\mathrm{A}}$; at the PH group is a 3 p AO of $\mathrm{P}_{\mathrm{C}}$ in the direction of the threefold axis of the trigonal pyramidal bonded phosphorus. While the Lp contribution at $\mathrm{P}_{\mathrm{C}}$ has a $3 p_{z} \mathrm{AO}$ character in 3exo and combines bonding with the $\pi\left(\mathrm{P}_{\mathrm{B}}, \mathrm{P}_{\mathrm{B}}\right)$ group orbital, it is of $3 p_{x}$ type in 3endo and is antibonding with respect to $\pi\left(\mathrm{P}_{\mathrm{B}}, \mathrm{P}_{\mathrm{B}},\right)$. In MO 20a' of 2endo the coefficients of the magnetically shielding Lp at $\mathrm{P}_{\mathrm{C}}$ is smaller than that in 2exo. This partially rationalizes that $\mathrm{P}_{\mathrm{C}}$ is so much less shielded (downfield) in 2endo than in 2exo. A simple explanation of this remarkable effect by a chargeshift relation is obviously wrong for 2 (Mulliken charges, $\delta^{31} \mathrm{P}$ pairs: $+0.05 /-120$ for $\mathrm{P}_{\mathrm{C}}$, exo; -0.60/-16 for $\mathrm{P}_{\mathrm{A}}$, exo; -0.63/ 221 for $\mathrm{P}_{\mathrm{A}}$, endo; -0.08/350 for $\mathrm{P}_{\mathrm{C}}$, endo) as well as for 3 ($0.40 /-78$ for $\mathrm{P}_{\mathrm{A}}$,exo; -0.48/377 for $\mathrm{P}_{\mathrm{A}}$, endo).

The endo/exo orientation of the exocyclic PH group in $\mathbf{3}$ effects only $\mathrm{P}_{\mathrm{A}}$ considerably. Does this mean that the phosphirene moiety is not involved? Again, the WBI are considered to get hints: $\mathrm{WBI}\left(\mathrm{P}_{\mathrm{A}} \mathrm{P}_{\mathrm{C}}\right)=0.98$ and 0.90 for $\mathrm{P}_{\mathrm{B}} \mathrm{P}_{\mathrm{C}}$ are in agreement with single bonds; remarkably, $\mathrm{WBI}\left(\mathrm{P}_{\mathrm{B}} \mathrm{P}_{\mathrm{B}},\right)$ is much closer to 1 than to 2 ( 1.33 3endo, 1.32 3exo); strikingly, there are one third bonds between $\mathrm{P}_{\mathrm{A}}$ and $\mathrm{P}_{\mathrm{B}}, \mathrm{P}_{\mathrm{B}}$, respectively ( $\mathrm{WBI}=0.38$ in 3endo, 0.37 in 3exo). These bonds towards the $\mathrm{P}_{\mathrm{B}} \mathrm{P}_{\mathrm{B}}$, fragment rationalize the $\delta^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{B}}\right)$ at -268 (3endo) and -247 (3exo), which are distinctly different from those of molecules with an unperturbed $\pi_{\mathrm{PP}}$ bond (trans- $\mathrm{H}-$ $\mathrm{P}=\mathrm{P}-\mathrm{H}$ with $\delta^{31} \mathrm{P}=407, \delta^{31} \mathrm{P}$ of $\sigma^{2}-\mathrm{P}$ in 1-X-phosphirenes with $\mathrm{X}=\mathrm{H}: 276 \mathrm{X}=\mathrm{PH}_{2}: 300$, and $\mathrm{X}=\mathrm{SiH}_{3}: 287$ calculated at GIAO/MP2/6-311G(d) on MP2/6-31G(d) geometries). The MOs 21a', 20a', and 19a' of the $C_{s}$ symmetric geometries contribute to this conjugation of $\mathrm{P}_{\mathrm{B}} \mathrm{P}_{\mathrm{B}}$, with the exocyclic PH group in both isomers, 3endo and 3exo. Since the order and shape of the symmetry orbitals in 3endo and 3exo appear to be the same, the large endo/exo effect in $\delta^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{A}}\right)$ seems puzzling. The endo/exo effect occurs also in the isovalent 1-thiophosphirene, but $\mathrm{P}_{\mathrm{B}} \mathrm{P}_{\mathrm{B}^{\prime}}$ is less pronounced (the sulfur in the endo isomer is 148 ppm less shielded than in the exo form). Since the set of MOs for $\mathrm{P}_{3}$-SH only differ in their AO coef-


6


8



9


11




15


Figure 4 Structures of $\mathrm{HP}_{4} \mathrm{Na}$
ficients but not in their character from those in the $\mathrm{P}_{3}-\mathrm{PH}$ isomers, $\mathbf{3}$, it is reasonable that both molecules show the outstanding endo/exo effect in the chemical shift of the exocyclic group. Since the a" symmetric MOs are not likely to change much from endo to exo, the following consideration focuses on the a' MOs, MO 20a' and MO 21a' especially.

The HOMO-2, 20a', and HOMO-1, 21a', can be constructed from a $\pi\left(\mathrm{P}_{\mathrm{B}} \mathrm{P}_{\mathrm{B}}\right)$ and a fragment orbital of the $\mathrm{P}_{\mathrm{C}} \mathrm{P}_{\mathrm{A}} \mathrm{H}$ part. While for both isomers of $\mathbf{3}$ in MO 21a' the $\pi\left(\mathrm{P}_{\mathrm{B}} \mathrm{P}_{\mathrm{B}}\right)$ ) is in z direction (with the $\mathrm{P}_{\mathrm{B}} \mathrm{P}_{\mathrm{B}}, \mathrm{P}_{\mathrm{C}}$ plane as nodal plane) the $\pi\left(\mathrm{P}_{\mathrm{B}} \mathrm{P}_{\mathrm{B}^{\prime}}\right)$ in MO 20a' is basically oriented in x direction (nodal plane perpendicular to the line from $\mathrm{P}_{\mathrm{C}}$ to the middle of $\mathrm{P}_{\mathrm{B}}$ and $\mathrm{P}_{\mathrm{B}}$, . The $\mathrm{P}_{\mathrm{C}} \mathrm{P}_{\mathrm{A}} \mathrm{H}$ fragment in 20a' mainly contributes a $p_{x}$ AO at $\mathrm{P}_{\mathrm{C}}$ to the MO, so that $\mathrm{P}_{\mathrm{A}}$, for which the endolexo effect
is obtained, is only slightly involved. In contrast, MO 21a' shows a principally different electronic structure at $\mathrm{P}_{\mathrm{A}}$ in the endo than in the exo isomer. The 'normal' fragment orbital of $\mathrm{P}_{\mathrm{C}} \mathrm{P}_{\mathrm{A}} \mathrm{H}$ appears in the exo isomer: a $\sigma\left(\mathrm{P}_{\mathrm{C}} \mathrm{P}_{\mathrm{A}}\right)$ mixing with the $\mathrm{s}(\mathrm{H}) \mathrm{AO}$ so that the outer lobe at $\mathrm{P}_{\mathrm{A}}$ mixes bonding with $\mathrm{s}(\mathrm{H})$. Like in a hydrogen bridged structure, the $\mathrm{P}_{\mathrm{C}} \mathrm{P}_{\mathrm{A}} \mathrm{H}$ fragment orbital in 3endo is composed of a $\sigma\left(\mathrm{P}_{\mathrm{C}} \mathrm{P}_{\mathrm{A}}\right)$ with the $\mathrm{s}(\mathrm{H})$ conjugate to the central lobe of the P-P $\sigma$ bond orbital. The combination of the $\mathrm{P}_{\mathrm{B}} \mathrm{P}_{\mathrm{B}}$, and the $\mathrm{P}_{\mathrm{C}} \mathrm{P}_{\mathrm{A}} \mathrm{H}$ group orbitals has antibonding character in MO 21a' (shortening the $\mathrm{P}_{\mathrm{B}} \mathrm{P}_{\mathrm{B}}$, but widening $\mathrm{P}_{\mathrm{B}} \mathrm{P}_{\mathrm{C}}$ ) in the endo as well as the exo isomer of 3 . Nevertheless, the hydrogens $P_{A}-P_{C}$ bridging valence in the endo isomer in contrast to having P-H bond character is probably the main reason for the remarkably different magnetic properties of $\mathrm{P}_{\mathrm{A}}$ in 3endo compared to 3exo. As mentioned above, only the calculated shifts of $\mathrm{P}_{\mathrm{B}}$ and $\mathrm{P}_{\mathrm{C}}$ of $\mathbf{3}$ endo and 3exo are in reasonable agreement with the measured values, while both $\delta^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{A}}\right)$ deviate distinctly: one too high, the other too low. Since the exocyclic group of $\mathbf{3}$ is able to rotate, an average $\delta^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{A}}\right)$ value should be considered, which comes close to the experimental chemical shift.

The predicted set of $\delta^{31} \mathrm{P}$ values for the lowest energy $\mathrm{HP}_{4}^{-}$ isomer, $\mathbf{1}$, is similar to those for the experimentally known compounds with the triphosphaallyl moiety (Table 1), but they do not match the experimental data for $\mathrm{HP}_{4}(\mathrm{Na} / \mathrm{K})$ solution. In disfavor of the bicyclic structure, the $\delta_{\text {calc }}{ }^{31} \mathrm{P}$ of 2 exo also shows distinct deviations ( $\Delta \delta^{31} \mathrm{P}=-119$ to +200 ppm ) from the experimental value. Remarkably, $\delta_{\text {calc }}{ }^{31} \mathrm{P}$ of the until now ignored structure 3 resembles the experimental results if rotational averaging is considered. Nevertheless, a question of interest is whether the remaining deviations, are due to coordination of a cation to the anionic phosphorus?

## Counterion effect

Since in the experimental work the $\mathrm{HP}_{4}{ }^{-}$anions were generated in $\mathrm{Na}^{+}$-containing solution and $\mathrm{HP}_{4} \mathrm{Na}^{+}$was detected in the mass spectrometer, the counterion effect of one sodium was studied (structures 6 to 16, Figure 4). Coordinating $\mathrm{Na}^{+}$ to the lone pair of the anionic phosphorus, $\operatorname{Lp}\left(\mathrm{P}_{\mathrm{A}}\right)$, and additionally to the tricoordinate $\mathrm{P}_{\mathrm{C}}$ of 2exo has the most stabilizing effect. The amount of stabilization can be estimated to be $35 \mathrm{~kJ} \mathrm{~mol}^{-1}$ from comparing the relative energies of $\mathbf{1}$ with 2exo $\left(\mathrm{E}_{\text {rel }}=23\right)$ and $\mathbf{6}$ or $\mathbf{7}\left(\mathrm{E}_{\text {rel }}=12.9 \mathrm{~kJ} \mathrm{~mol}^{-1}\right)$ with $\mathbf{1 1}$. Coordination of sodium to one $\mathrm{Lp}\left(\mathrm{P}_{\mathrm{A}}\right)$ and the $\mathrm{P}_{\mathrm{B}}-\mathrm{P}_{\mathrm{B}}, \pi$ bond is less effective but provides the minimum 11, which is about as stable as $\mathbf{6}$ or $\mathbf{7}$, the $\pi$ complexes of $\mathbf{1}$ with $\mathrm{Na}^{+}$. Within the set of $\mathrm{HP}_{4} \mathrm{Na}$ with the bicyclo $\mathrm{P}_{4}$ framework structure $\mathbf{1 1}$ is followed by $\mathbf{1 2}$ and $\mathbf{8}$ on the energy scale. In 8 and $\mathbf{1 2}, \mathrm{Na}^{+}$is attached to $\mathrm{P}_{\mathrm{A}}$ in an exo position and the exo preference of the P-H bond is slightly larger $\left(4.0 \mathrm{~kJ} \mathrm{~mol}^{-1}\right)$ than in $2(1.4 \mathrm{~kJ}$ $\mathrm{mol}^{-1}$ ). The higher relative energy of 9 can be rationalized by steric hindrance of hydrogen and sodium being both in endo conformations. Isomer $\mathbf{1 0}$ has no $\mathrm{P}_{\mathrm{A}}$ - Na contact but only coordination of $\mathrm{Na}^{+}$to a neutral tricoordinate phosphorus and is therefore relative high in energy ( $117.1 \mathrm{~kJ} \mathrm{~mol}^{-1}$ ). The energetic ordering of the sodium complexes is found as fol-
lows: $\mathbf{1 1}<\mathbf{1 2}<\mathbf{8}<\mathbf{9} \ll \mathbf{1 0}$. In contrast to the $\mathrm{HP}_{4} \mathrm{Li}$ study [4] based on RHF/DZP optimizations, the ' 'endo $+\mathrm{Na}^{+}$" has only one valence isomer, 8. Nevertheless, the relative energies $\left(0.0<43.9<48.9<49.8 \ll 154.8 \mathrm{~kJ} \mathrm{~mol}^{-1}\right.$ ) of the corresponding $\mathrm{HP}_{4} \mathrm{Li}$ structures [4] reflect similar stabilization effects as in the $\mathrm{HP}_{4} \mathrm{Na}$ isomers $\mathbf{8 - 1 2}$ (Table 3). With the exception of 16, the $\mathrm{HP}_{4} \mathrm{Na}$ structures based on the $\mathrm{HP}_{4}$ - framework of $\mathbf{3}$ have relatively high energies ( 65.9 for $\mathbf{1 5}$ to 89.2 $\mathrm{kJ} \mathrm{mol}^{-1}$ for 13). This indicates that $\mathrm{Na}^{+}$coordination to the triphosphirene ring is not very efficient, although it has a $\pi$ bond group orbital.

The $\delta^{31} \mathrm{P}$ data for the $\mathrm{HP}_{4} \mathrm{Na}$ structures listed in Table 3 confirm that the isomer with the triphosphaallyl moiety was not observed [5] in the experiment. The changes of $\delta^{31} \mathrm{P}$ from $\mathbf{1}$ to $\mathbf{6}$ or $\mathbf{7}$ are astonishingly small: for $\mathrm{P}_{\mathrm{A}}-19$ and -106 ppm , for $P_{C}+2$ and -13 , and for $P_{B}+47(1$ to $\mathbf{6})$ and no change from 1 to 7. In contrast, the allylic $P_{A}-P_{B}$ bond length is more sensitive to the counterion than to the link group X in cyclo-$1,2,3-(\mathrm{P})_{3} \mathrm{X}$ (with $\mathrm{X}=\mathrm{PH}, \mathrm{CH}_{2}$, as compared to the acyclic R-PPP-R [7] anion). Therefore, compensation of effects is likely to be responsible for the moderate changes of $\delta^{31} \mathrm{P}$ for $\mathbf{1}, \mathbf{6}$, and 7. The effect of $\pi$-coordination of $\mathrm{Na}^{+}$on $\delta^{31} \mathrm{P}$ is larger for $\mathbf{3}$ (e.g. $\delta^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{B}}\right)$ changes from -288 (3endo) to -204 ppm in 13). Noteworthy, coordination of $\mathrm{Na}^{+}$to the $\pi$ bond at the anti position to the phosphido group has quite a large effect on $\delta^{31} \mathrm{P}$ of the remote phosphorus $\left(\delta^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{A}}\right): 319\right.$ in 3endo and 438 in 13). On the other hand, coordination of $\mathrm{Na}^{+}$to either side of the $\pi$ bond of 3exo gives rise to small down field changes ( $\delta^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{A}}\right):-98$ (3exo) to -20 (14) and -35 for 16). Is the effect of the $\mathrm{Na}^{+}$additive? In GIAO /MP2 calculations with the $6-31 \mathrm{G}(\mathrm{d})$, which is a smaller basis set than used throughout this study, the $\delta^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{A}}\right)$ is 50 for a $\mathrm{HP}_{4} \mathrm{Na}_{2}{ }^{+}$ structure in which the sodiums are placed as in $\mathbf{1 4}$ and $\mathbf{1 6}$. Therefore, further research for $\mathbf{3}$ might focus on $\left[\mathrm{HP}_{4}{ }^{-*} \mathrm{Na}^{+} . \infty\right.$ chains with this building block.

The bicyclo- $\mathrm{P}_{4}$ based $\mathrm{HP}_{4} \mathrm{Na}$ structures have a $\delta^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{B}}\right)$ in the small range of -367 to -285 ppm . This means that the counterion effect on the central $P_{B}$ is quite small. Even in $\mathbf{8}$ and 12, where $\mathrm{Na}^{+}$is close to $\mathrm{P}_{\mathrm{B}}\left(\mathrm{Na}-\mathrm{P}_{\mathrm{B}}=2.922 \AA\right.$ in $\mathbf{8}$ and 2.918 in 12), $\delta^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{B}}\right)$ is about the same as in the parents 3endo and 3exo. In all $\mathrm{HP}_{4} \mathrm{Na}$ with bicyclo- $\mathrm{P}_{4}$ backbone $\delta^{31} \mathrm{P}$ of the anionic phosphorus, $\mathrm{P}_{\mathrm{A}}$, changes to higher field when $\mathrm{Na}^{+}$is coordinated to it. This effect ranges from $\Delta \delta^{31} \mathrm{P}(2$ endo to $\mathbf{9})=-38$ to $\Delta \delta^{31} \mathrm{P}(\mathbf{2}$ exo to $\mathbf{8})=-77 \mathrm{ppm}$. With the exception of $\mathbf{1 0}, \mathrm{Na}^{+}$is never coordinated to $\mathrm{P}_{\mathrm{C}}$, in the [ $\mathbf{2} * \mathrm{Na}$ ] complexes] Consequently, $\delta^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{C}}\right)$ is only slightly affected by the counterion] Since $\mathrm{Na}^{+}$interacts only in $\mathbf{1 1}$ with the $\mathrm{Lp}\left(\mathrm{P}_{\mathrm{A}}\right)$ the counterion effect on $\delta^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{A}}\right)$ is larger in 11 than in 8-10 and $\mathbf{1 2}$ (Tables 1 and 3). In general, the $\mathrm{Na}^{+}$has a small effect on the NMR chemical shifts of $P_{A}$ and $B_{C}$ in the conjugate system and systematically changes $\delta^{31} \mathrm{P}$ to lower field in the phosphanidophosphirene, so that the endol exo difference remains. Nevertheless, the computed effects of $\mathrm{Na}^{+}$ on $\delta^{31} \mathrm{P}$ in $\mathrm{HP}_{4}{ }^{-}$ions are in agreement with the re-assignment of the experimental values to the phosphirenylphosphide structure, 3.

## Summary

The energy difference between the bi- and monocyclic $\left(\mathrm{P}_{3} \mathrm{X}^{-}\right.$ anions with $\mathrm{X}=\mathrm{PH}$, or $\mathrm{CH}_{2}$ are in agreement with the 'allyl preference', which was recently reported for the acyclic triphosphide, R-PPP- $\left.\mathrm{R}^{-}\right]$The $\delta^{31} \mathrm{P}$ values predicted for the preferred structure of the $\mathrm{HP}_{4}{ }^{-}$anion does not agree with the reported NMR chemical shifts for $\mathrm{HP}_{4}(\mathrm{Na} / \mathrm{K})$. Even when considering the counterion effect, the computed $\delta^{31} \mathrm{P}$ values disagree with an assignment to $\mathbf{1}$ to a four-membered ring structure. Out of a variety of $\mathrm{HP}_{4} \mathrm{Na}$ structures, which comprise a bicyclo[1.1.0] $\mathrm{P}_{4} \mathrm{H}^{-}, \mathbf{2}$, or a $\mathrm{P}_{3}-\mathrm{PH}^{-}, \mathbf{3}$, structure, the latter provides better agreement with the $\delta_{\text {exp }}{ }^{31} \mathrm{P}$ values. The $\delta_{\text {calc }}{ }^{31} \mathrm{P}$ of the exocyclic PH group in $\mathbf{3}$ shows distinct deviations ( 306 in 3endo, -149 ppm in 3exo) from the probably related experimental chemical shift, $\delta_{\text {calc }}{ }^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{A}}\right)$. Nevertheless, due to a low rotation barrier between 3endo, and 3exo) an average $\delta^{31} \mathrm{P}\left(\mathrm{P}_{\mathrm{A}}\right)$ has to be considered in favor of structure 3.

From the $\delta_{\text {calc }}{ }^{31} \mathrm{P}$ values for a comprehensive set of phosphanide molecules at the MP2 and the DFT levels and the $\mathrm{HP}_{4} \mathrm{Na}$ calculations conclusions can be drawn on the performance of the NMR methods and the counterion effect: a) $A b$ initio NMR method: for localized structures, the DFTderived $\delta^{31} \mathrm{P}$ differ by only +8 to +36 ppm from the MP2 values. However, deviations of up to 242 ppm occur for structures with $\pi_{\mathrm{pp}}$ bonds. b) Counterion effect: probably due to the neglect of counterion effects, most $\delta_{\text {calc, MP2 }}{ }^{31} \mathrm{P}$ values are at higher field than $\delta_{\text {exp }}{ }^{31} \mathrm{P}$ of related compounds. This is confirmed as a trend by the $\delta_{\text {calc }}{ }^{31} \mathrm{P}$ of $\mathrm{HP}_{4} \mathrm{Na}$ structures. We are aware of the difficulties related to the synthesis of phosphanide compounds but hope that the presented chemical shifts can be of help in identifying the fascinating triphosphaallyl moiety (e.g. in cyclo- $\mathrm{P}_{3}(\mathrm{CH})_{2}{ }^{-}$) if they appear intermediately in the experiment.

Acknowledgements The authors thank various Flemish science foundations (FWO-Vlaanderen, GOA-Program, and KULeuven Research Council) for continuing support and J. Hahn, K. Karaghiosoff, and D. Gudat for sharing their profound knowledge of ${ }^{31} \mathrm{P}$ NMR. Furthermore, inspiring discussions with A. Wörner are acknowledged here.

Supplementary material available 3D coordinates of the molecules from Table 1-3 in XYZ format with the calculated isotropic magnetic shielding as fourth coordinate; 3D representation of the MOs with 20a' and 21a' symmetry of 3endo and 3exo in VRML format; Gaussian output of 1, $2 e n d o, 2 e x o, 3 e n d o$ and 3exo.

The SHARC files, containing computed magnetic shielding tensors, are available from the author upon request (please contact Alk Dransfeld:
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For more information on NMR-SHARC see
http://www.ccc.uni-erlangen.de/sharc/
or http://www.quantchem.kuleuven.ac.be/sharc/

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    Dedicated to Professor Paul Ragué von Schleyer on the occasion of his $70^{\text {th }}$ birthday

